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Comparison of methods to estimate areal means of short duration rainfalls in small catchments, using rain gauge and radar data

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19 **Abstract**

20

21 Flood forecasting for early alerts is a challenging task for hydrologists. This is particularly the case in small
22 catchments due to a lack of upstream gauges and their flashy response. In such catchments, estimating areal
23 mean rainfall at short intervals by applying spatial interpolation schemes based on rain gauge data in short
24 time scales is a significant work for accurate flood forecasting. In this study, we compare and evaluate four
25 commonly used spatial interpolation methods in small catchments, which have small numbers of rain gauges
26 in South Korea. We investigate the impacts of catchment area on different spatial interpolation schemes. Then a
27 simulation is done with hypothetical storms to illustrate the limitation of the Thiessen method. Local heavy rainfall
28 events have been selected for case studies and 10-minute rain gauge rainfall data are used, since short time
29 scales of rainfall data are generally needed for flash flood forecasting and alerts. Furthermore, we analyse the
30 characteristics of different spatial interpolation techniques by comparing the results with weather radar rainfall.
31 The results revealed that mean absolute percentage discrepancy (MAPD) of areal mean rainfall between the
32 Thiessen polygon method and the other three interpolation schemes (Inverse distance weighting, Multiquadric
33 interpolation, Kriging) increases rapidly as the catchment area becomes smaller, especially when the
34 catchment area is less than $500km^2$. In addition, regarding the number of rain gauges in a catchment, the
35 smaller the number of rain gauges used in calculating areal mean rainfall, the larger the MAPD becomes, as
36 expected. Furthermore, the number of rainfall events with outliers increased as correlation among rain gauge
37 locations increased, which implies that outliers are more likely to happen when the gauges are located in a
38 linear format rather than in a cluster. Finally, the temporal distributions of areal mean rainfall obtained from
39 rain gauge and weather radar data are different depending on the direction of rainfall movement, especially in
40 sparsely gauged catchments. This study provides a possible guideline for rain gauge number and placement to
41 estimate areal mean rainfall accurately at small catchments.

42

43 Keywords: spatial interpolation method, Thiessen polygon, Inverse distance weighting, Multiquadric
44 interpolation, Kriging, radar rainfall

45

1. Introduction

Spatial distribution of precipitation data plays an important role in many environmental applications, especially for water resources (Chen et al., 2017; Faurès et al., 1995; Li and Heap, 2011; Ly et al., 2011; Wagner et al., 2012). Hydrologists need accurate spatial rainfall data across a catchment for hydrological risk assessment and water budget estimates. Most of the precipitation data are collected by geographically dispersed networks of rain gauges, which are point data. Rain gauges provide comparatively accurate measurement of precipitation at a point, however, they cannot fully capture the spatial variability of rainfall with time due to its temporal and spatial variability. The rain gauge data are generally used as inputs to hydrological models and the model accuracy is influenced significantly by these input data (Beven, 2011). Especially, the quality of hydrological model result depends on the quality of continuous spatial rainfall data (Andréassian et al., 2001; Kobold and Sušelj, 2005; Leander et al., 2008; Moulin et al., 2009; Singh, 1997). The use of a small number of rain gauge data may cause great uncertainties in simulated streamflow (Chaubey et al., 1999; Faurès et al., 1995), particularly when the rain gauge stations are placed outside the studied catchment (Schuurmans and Bierkens, 2006).

Various spatial interpolation schemes have been developed and applied ranging from simple methods such as Thiessen polygons (Thiessen, 1911) and Inverse Distance Weighting (IDW) (Berndt and Haberlandt, 2018; Di Piazza et al., 2011; Teegavarapu et al., 2009) to more complex methods such as Kriging which incorporate secondary information (e.g., elevation, remotely sensed observation, etc) as covariates to improve primary data. The former and the latter are also known as deterministic methods and geostatistical methods respectively (Ly et al., 2011). Conditional merging (CM) techniques have been developed which are methods of spatial interpolation suited for merging spatially continuous grid-based measurements and point measurements (Pegram, 2001; Sinclair and Pegram, 2005). The CM preserves the spatial covariance structure of spatially continuous grid-based measurements while maintaining the accuracy of the point-based measurements. Numerous comparative studies have been done to explore which spatial interpolation method for rain gauge data is the best, however there were no consistent findings (Dirks et al., 1998; Oke et al., 2009; Otieno et al., 2014; Price et al., 2000; Vicente-Serrano et al., 2003; Zimmerman et al., 1999), indicating that more studies are needed in this field. Interpolating rain gauge rainfall is a challenging task since the

73 application of different methods may cause different results from the actual spatial distribution of rainfall,
74 which is of course unknown.

75 In most studies, spatial interpolation techniques have been applied to daily, monthly and annual time steps of
76 rainfall data (Ly et al., 2013) and only a few studies have compared interpolation methods using hourly time
77 steps, e.g., Schiemann et al (2011). Moreover, few studies have compared interpolation schemes based at a
78 sub-hourly time scale. Normally the spatial variability of rainfall is more obvious at shorter time scales,
79 therefore simple spatial interpolation of rainfall may not yield an accurate measurement of the real rainfall
80 field. This was demonstrated by Haylock et al (2008) and Yatagai et al (2009).

81 Recently, radar rainfall data have been used frequently as inputs for hydrological applications (Fassnacht et al.,
82 2003; Neary et al., 2004; Tetzlaff and Uhlenbrook, 2005), especially in urban hydrology owing to the
83 advances in technologies, numerical models, and data processing (Thorndahl et al., 2017). Unlike rain gauge
84 data, weather radars can survey large areas and can better capture the spatial variability of rainfall fields
85 (Ochoa-Rodriguez et al., 2019). However, they are often biased due to various factors such as topography,
86 climate and spatio-temporal resolution (Ebert et al., 2007; Karimi and Bastiaanssen, 2015; Maggioni et al.,
87 2016). The rain intensity is derived indirectly from the measurement of reflectivity, hence, the data is subject
88 to systematic and random errors such as instrumental and sampling error especially in mountainous terrain
89 (Gabella et al., 2005). In addition, radar rainfall amount is normally smaller than the rain gauge rainfall
90 amounts (Smith et al., 2007) due to the difference in spatial domains. The typical pixel size of conventional
91 weather radars is 1×1 km or 2×2 km whereas the sample area of a rain gauge is typically 200-300 cm².

92 Flood forecasting for early warning is a challenging task for hydrologists. This is particularly the case in small
93 catchments due to a lack of upstream stream gauges and flashy rainfall-runoff response (i.e., short lead time).
94 In such catchments, estimating areal rainfall by applying spatial interpolation schemes using rainfall data from
95 rain gauges in short time scales (e.g. 10-minute) is valuable for accurate flood forecasting. Recently, there has
96 been an increasing trend of localized torrential rainfall events in summer in South Korea (Boo et al., 2006;
97 Chang and Kwon, 2007). In this context, we compare and evaluate spatial interpolation methods in small
98 catchments which have a small number of rain gauges in South Korea. Local heavy rainfall events have been

99 selected for case studies and 10-minute rain gauge rainfall data are used, since short time scales of rainfall
100 data are generally needed for flash flood forecasting and alerts. Furthermore, we analyse the characteristics of
101 different spatial interpolation techniques by comparing the results with radar rainfall.

102 Given this background, this paper explores the following questions:

- 103 (1) For flood forecasting, are deterministic spatial interpolation methods appropriate for small
104 catchments with sparse rain gauge networks? If not, what are the limitations?
- 105 (2) What are the effects of rain gauge density, rain gauge distribution and rainfall direction on different
106 spatial interpolation schemes? Are there any correlations between rain gauge density and outliers in
107 rainfall data?
- 108 (3) Can weather radar rainfall be a useful alternative to rain gauge data at regional-scale catchments with
109 low densities of rain gauges?

110 The primary objectives addressed in this paper are to: (1) assess the effects of catchment area, rain gauge
111 density, rain gauge distribution and direction of rainfall movement on estimating areal average rainfall with
112 different spatial interpolation methods and (2) suggest guidelines for rain gauge numbers and placement to
113 estimate accurate areal mean rainfall on small catchments. This investigation has both practical and scientific
114 value since it allows us to identify not only the importance of physical characteristics (i.e., number and
115 location) of rain gauges but also the effects of rainfall movement and direction in estimating areal mean
116 rainfall.

117 In Section 2, we describe the study area, rain gauge and radar rainfall data used. Spatial interpolation schemes
118 used in this study are briefly introduced in Section 3. The impacts of catchment area, rain gauge density and
119 rainfall direction on spatial interpolation methods are presented in Section 4. The main conclusions of this
120 study are summarized in Section 5.

121

122 **2. Catchment and data**

123 **2.1 Study area**

124 The basins (catchments) of South Korea are classified into three groups: 21 large sized areas (Basin), 117
125 medium sized areas (Sub-basin) and 850 small sized areas (Standard-basin) as shown in Figure 1. Basins are
126 divided according to the 5 largest rivers (Han River, Nakdong River, Geum River, Seomjin River, and
127 Yeongsan River), coastal areas and Jeju Island. Each Sub-basin is divided based on the confluences of natural
128 rivers and the major islands of the southern and western sea. Lastly, Standard-basins are divided on the basis
129 of the point where national and regional rivers gather, the point where a dam is located and the area where
130 major facilities that manage waters are located.

131

132 **2.2 Precipitation data**

133 **2.2.1 Rain gauge data**

134 Two sources of rain gauge data are used in this study. First, Automatic weather stations (AWS) installed by
135 the Korea Meteorological Administration (KMA) are used. Daily rainfall data from 2001 to 2010 are used to
136 make $5\text{km} \times 5\text{km}$ grid rainfall. These data are used to analyse differences among spatial interpolation methods
137 with regard to catchment area in Section 4.1. Figure 1(a) shows the distribution of 515 AWS and 117 sub-
138 basins.

139 AWS installed by KMA are quite evenly distributed over South Korea. However, since AWS distribution is
140 based on administrative district, the AWS network is weak in considering catchment characteristics. Therefore,
141 another set of rain gauge data from the Ministry of Environment (ME), which are installed based on
142 catchment size and used in river flood forecasting, are used instead of AWS data in Section 4.2. 10-minute
143 rainfall data from 2016 to 2018 is used to compare the estimated areal mean rainfall difference between spatial
144 interpolation methods when the rain gauge density changes. Figure 1(b) shows the locations of 664 standard-
145 basins and 564 rain gauges installed by ME, which are used in river flood forecasting.

146 [Insert Figure 1]

147

2.2.2 Weather radar rainfall data

Weather radar data are received from 1 single polarization radar (Imjin) and 5 dual polarization radars (Biseul, Sobaek, Gari, Seodae, Mohu) operated by the Flood Control Office of ME (Ministry of Environment of Korea), which have temporal and spatial resolutions of 10-minute and 250m respectively. In this study, the Marshall and Palmer equation (Marshall and Palmer, 1948) is applied for single polarization radar quantitative precipitation estimation (QPE) and the JPOLE algorithm (Ryzhkov et al., 2005) is used for dual polarization radar QPE. The coverage and distribution of weather radars in South Korea are shown in Figure 2.

[Insert Figure 2]

3. Spatial interpolation schemes

We used four common interpolation techniques: Thiessen polygon, Inverse distance weighting, Multiquadric interpolation and Kriging methods. Brief introductions to the spatial interpolation schemes applied in this study are provided here, since details on various methods are available from many hydrological and statistical textbooks. In South Korea, the Thiessen polygon method is officially used for river flood forecasting, hence, differences of estimated areal mean rainfall between the Thiessen polygon method and the other three methods are compared in this study. We regenerated 495km (longitude direction) \times 725km (latitude direction) grid rainfall at 5km intervals using 10-minute rainfall data. Four different interpolation schemes are applied and the areal mean precipitation is estimated by averaging the grid rainfall.

Thiessen polygon (TSN)

The catchment area is divided into polygons with each polygon containing a rain gauge (a single point of sampling) (Chow, 1964). Each polygon represents the entire area covered by that polygon. Although this is a simple and straightforward method, it has some disadvantages. For example, the estimation is based on only a

single gauge and does not incorporate the information on neighbouring points. In addition, there are sudden jumps or discontinuities across the boundaries of polygons.

173

174 **Inverse Distance Weighting (IDW)**

IDW estimates the value at an unsampled site by the distance weighted average of observed data from all sampled sites surrounding it. As the distance increases between the unknown value of the estimated point and the surrounding known sampled points, the weight decreases which means that the interpolant is less influenced by the sampled value. The weight λ_i is calculated as

$$179 \quad \lambda_i = \frac{D_{0i}^{-d}}{\sum_{j=1}^n D_{0j}^{-d}}$$

where D_{0i} is the distance from the sampled point to the estimated point, d is the geometric form of the weight, n is the number of known value locations. The power d was set to 2, which was found not to be significantly different from the results realized by optimal power values (Otieno et al., 2014).

183

184 **Multiquadric Interpolation (MQI)**

The MQI was first developed by Hardy (Hardy, 1971) for the interpolation of irregular surfaces in geophysical sciences. Then it was applied to rainfall surfaces with the satisfactory result for determining areal rainfall (Shaw and Lynn, 1972). Multiquadric analysis represents the surface to be approximated as a summation of a number of individual quadric surfaces. The catchment perimeter is determined by a polygon of m sides whose vertices are given by the pairs (x_k, y_k) , $k=1,2,...,m$. Inside and outside this polygon are n rain gauges whose coordinates are (g_i, h_i) , $i=1,2,...,n$. A rainfall amount is recorded at each rain gauge, and the amount is given as z_i . Multiquadric hyperboloids centered at each rain gauge take the following form:

$$192 \quad z_i = \sum_{j=1}^n [(g_j - g_i)^2 + (h_j - h_i)^2 + a^2]^{1/2} c_j$$

193 A number of researchers have used MQI (e.g. Pegram and Pegram, 1993) and readers are referred to the
194 papers cited above for the details about this method.

195

196 **Kriging (KRG)**

197 In this study Ordinary Kriging (Wackernagel et al., 1997) is used which is the standard version of Kriging.
198 KRG is categorized as a univariate approach since no additional information is considered except for one data
199 source. The KRG estimate at a point u_0 is calculated as follows:

$$200 \quad Z^*(u_0) = \sum_1^n \lambda_i Z(u_i)$$

201 where, λ_i is the weight of each of the n adjacent observations taken into account. The weights are obtained by
202 solving the kriging system:

$$203 \quad \sum_{j=1}^n \lambda_j \gamma(u_i - u_j) + \mu = \lambda \gamma(u_i - u_0) \text{ for } i=1, \dots, n, \quad \sum_{j=1}^n \lambda_j = 1$$

204 here, μ is a Lagrange multiplier. Kriging requires a variogram model to estimate its weights. In this study, the
205 least squares method has been applied due to its computational simplicity and broad availability. The least
206 squares variogram parameter estimates are those that minimize the squared differences between the
207 experimental variogram and theoretical model. In this study, the spherical model was adopted to perform a
208 least squares fit of theoretical variograms to an experimental variogram. In order to perform semivariogram
209 analysis and subsequent KRG, GSTAT software (Pebesma and Wesseling, 1998) was used. The estimated
210 correlation distance varies depending on the regions and events. In this study, it was set in the range of 20 to
211 40 km.

212

213 **4. Results and discussion**

214 The first part of this section investigates the impacts of catchment area on different spatial interpolation
215 schemes. Then a simulation is done with hypothetical storms to illustrate the limitation of TSN by presenting

the effects of rain gauge distribution and storm direction on estimated areal mean rainfall when TSN is applied at small catchments. Finally, effects of rain gauge density, distribution and the direction of rainfall movement on spatial interpolation methods are explored with real recorded rainfall data at small catchments.

4.1 Effects of catchment area on spatial interpolation schemes

Areal mean annual rainfall (AMAR) in Mid-Sized catchments over South Korea is studied to explore the impact of catchment area on different spatial interpolation schemes. Mean absolute percentage discrepancy (MAPD) has been estimated with Equations (1) to (3) to compare against the TSN method. Among 117 Mid-Sized catchments in South Korea, the following types of catchments (66 Mid-Sized catchments) are excluded for consistent comparison: catchments that contain no rain gauges, catchments near the Demilitarized Zone, catchments near the complex coastline and catchments where mean elevation is higher than 400m.

$$MAPD_{IDW} = \frac{|AMAR_{TSN} - AMAR_{IDW}|}{AMAR_{TSN}} \times 100 \quad (1)$$

$$MAPD_{KRG} = \frac{|AMAR_{TSN} - AMAR_{KRG}|}{AMAR_{TSN}} \times 100 \quad (2)$$

$$MAPD_{MQI} = \frac{|AMAR_{TSN} - AMAR_{MQI}|}{AMAR_{TSN}} \times 100 \quad (3)$$

where, $AMAR_{TSN}$, $AMAR_{IDW}$, $AMAR_{KRG}$, $AMAR_{MQI}$ are areal mean annual rainfall obtained from TSN, IDW, KRG and MQI respectively. Figure 3 presents mean absolute percentage discrepancy (MAPD) of areal mean annual rainfall for different spatial interpolation schemes and catchment area. As shown in Figure 3, MAPD and catchment area are inversely proportional. In addition, the MAPD between TSN and the other three interpolation schemes increase rapidly as the catchment area becomes smaller, especially when the catchment area is less than $500km^2$ (shaded pink in the figure). This might be because normally small catchments in South Korea have complicated topography and low density of rain gauges. In the case of large catchments, differences tend to be less than 2% and almost constant, which means that there are no obvious distinctions among the four interpolation techniques.

[Insert Figure 3]

240 Since the differences between the four spatial interpolation schemes are large in catchments smaller than
241 500km², the drawbacks of applying different interpolation methods at small catchments are analysed in the
242 next section by illustrating a conceptual simulation for an example and presenting the result of real cases.

243

244 **4.2 Limitation of the spatial interpolation scheme on small catchments**

245 **4.2.1 Effects of rain gauge distribution and rainfall direction on TSN**

246 The flaw of TSN is demonstrated as an example in Figure 4. Let us assume that the four rain gauges (A, B, C
247 and D) are all located outside the catchment and the storm is moving, i.e. the rainfall direction is from South
248 West to North East (Case 1) and vice versa (Case 2). In Case 1, although the rainfall pass through the
249 catchment, the areal rainfall of the white hatched part of the catchment may not be estimated until the storm
250 arrives at Rain Gauge A, which is placed outside the catchment. As a result, in this case, peak rainfall will be
251 estimated later than the real peak rainfall. On the other hand, in Case 2, when the storm arrives at Rain Gauge
252 A, areal rainfall of the white hatched part of the catchment is computed even though the rainfall has not
253 arrived at the catchment yet. Consequently, in this case, peak rainfall will be estimated beforehand rather than
254 when the real peak rainfall occurs.

255 [Insert Figure 4]

256 As explained in the previous paragraph, TSN has structural limitations in estimating areal mean precipitation.
257 The following hypothetical example in Figure 5 also demonstrates the drawback of using TSN in calculating
258 areal mean precipitation. The experimental set up for this example is as follows:

- 259 - The unit of time and distance is ignored since this is a hypothetical example.
- 260 - The horizontal axis indicates the movement of rainfall and the vertical axis is the time scale.
- 261 - A spatial distribution pattern of the hypothetical rainfall is modeled in five horizontal grids, the
262 intensity of each grid having 5, 7, 10, 13 and the 7mm respectively. The storm is moving from left to
263 right with constant velocity, two grids at each time step.

- The distances between rain gauges are set further apart than the size of the storm (five grids) since the study case in this study is a small catchment with a low density of rain gauges.
- The region is divided into three sub-regions. On the horizontal axis, three hypothetical rain gauges (green vertical bars) (A, B, C) are in a line. The area of each sub-region is assumed to be the number of grid squares that each sub-region has. In this case, the area is 16, 11 and 18 for polygon A, B, and C respectively, as indicated by the red captions at the bottom of the figure.
- Since the total catchment area is 45, the areal proportion of each sub-region A, B and C is 0.36, 0.24 and 0.40 respectively.

Under these conditions, while the rainfall moves from left to right it will pass through rain gauge A, B and C in order and the areal mean rainfall will be estimated by the ratio of sub-region weight. Since the shape of storm and rainfall intensity remains unchanged, true areal mean rainfall should be constant regardless of time. However, when TSN is applied, since the distance between the rain gauges is larger than the size of the rainfall (5 grid squares), the areal rainfall of each sub-region is estimated only when the rainfall arrives at the gauge. Therefore, although the true areal mean rainfall is constant (GRD), the estimated areal mean rainfall is fluctuating sharply in a serrated shape (TSN) as shown in the right panel of Figure 5. For instance, when the center of the moving rainfall (i.e., the maximum value in this rainfall) just arrives on the rain gauge, areal mean rainfall may be overestimated with the value close to the point rainfall. On the other hand, if the rainfall is away from the rain gauge areal mean rainfall may be underestimated with the value of zero. As shown in this demonstration, TSN has structural limitations in computing areal mean rainfall, and therefore the amount of estimated areal mean rainfall might be distorted especially when the catchment is small and the rain gauge density is low.

[Insert Figure 5]

4.2.2 Effects of rain gauge density and Interpolation method

288 To demonstrate the effects of rain gauge density on estimated areal mean rainfall with different spatial
 289 interpolation methods applied, rainfall events in each of 664 Standard-basins between the year 2016 and 2018
 290 were selected and analysed. Six hundred and sixty four Standard basins were chosen from among all 850
 291 Standard-basins, since they are used for flood forecasting in South Korea. Rainfall events that meet the
 292 following two conditions in each Standard-basin are considered as outliers and have been excluded: (1)
 293 cumulative areal mean rainfall using radar rainfall data is less than 10mm; (2) estimated areal mean rainfall
 294 difference between using rain gauge data and radar rainfall data is larger than a factor of three. Finally, 528
 295 Standard-basins and 1404 rainfall events were chosen for areal mean rainfall analysis in this study. Figure 6
 296 shows the distribution of catchment area over the 528 standard-basins.

297 [Insert Figure 6]

298 Figure 7 shows how areal mean rainfall was modelled. To evaluate the effects of rain gauge density on areal
 299 mean rainfall calculated from four different interpolation methods, reference areal mean rainfall is needed. In
 300 this study areal mean rainfall estimated using radar rainfall data is set as a reference since radars can survey
 301 large areas and can better capture the spatial variability of rainfall fields (Ochoa-Rodriguez et al., 2019). Here,
 302 the bias of radar data was not adjusted by rain gauges for the following reasons: (1) the key process of
 303 correcting the bias of radar includes matching underlying statistical properties between the radar and rain
 304 gauge data. Therefore, the result of comparing different spatial interpolation methods may be distorted by a
 305 bias adjustment process, (2) adjusting radar rainfall estimates by rain gauge observations may not remove the
 306 bias entirely. Rainfall data is collected from rain gauges, and the corresponding radar rainfall estimate is taken
 307 from the radar grids, at a very large difference of scale, which is used to calculate areal mean rainfall. The
 308 mean absolute percentage error (MAPE) is commonly used in model evaluation, due to its intuitive
 309 interpretation in terms of relative error. Therefore, MAPE of four different interpolation methods is estimated
 310 as in Equation 4.

$$311 \quad MAPE_{ITP}^{RDR} = \frac{|AMR_{GRD}^{RDR} - AMR_{ITP}^{RDR}|}{AMR_{GRD}^{RDR}} \times 100 \quad (4)$$

312 where, the superscript RDR represents radar and ITP represents interpolation methods. TSN, IDW, KRG and
 313 MQI. AMR_{ITP}^{RDR} are areal mean rainfall estimates obtained from radar grids at corresponding rain gauge points

314 using *TSN*, *IDW*, *KRG* and *MQI* interpolation methods respectively. AMR_{GRD}^{RDR} is areal mean rainfall estimated
315 from radar grid rainfall.

316 [Insert Figure 7]

317 Figure 8 shows the MAPE with regard to the number of gauges used in estimating areal mean rainfall. The
318 box height represents the 25th percentile (1st quartile) to the 75th percentile (3rd quartile) of MAPE sets, which
319 is generally called as interquartile range (IQR). The mid horizontal line that goes through each box represents
320 the median and the black circle represents the mean value. The whiskers are the two lines outside the box that
321 extend to the highest and lowest value ($1.5 \times \text{IQR}$). The range of IQR and $1.5 \times \text{IQR}$ of IDW and KRG is less
322 than those of MQI and TSN when the number of rain gauge is less than two. However, when the number of
323 rain gauge is more than three, the differences among the four methods are not large. An interesting thing is
324 that, for MQI, when the rain gauge number is less than two, the range of IQR is the widest and the mean value
325 is the largest, while the median value is not that different from the other methods. This indicates that there are
326 some big storm events that affect MAPE and the mean value when MQI is applied, but in general, MAPE is
327 not that large compared with the other three methods.

328 [Insert Figure 8]

329 Analogous to other studies (Bárdossy and Pegram, 2013; Borga and Vizzaccaro, 1997), the performance of
330 the interpolation methods is dependent on the rain gauge density. As can be seen in Figure 9, areal mean
331 rainfall differences between the interpolation methods decrease as the number of rain gauges increase. The red
332 line with circular dots in Figure 9 shows the best fit line (the second degree polynomial equation) of the mean
333 value of MAPE. MAPE shows 20% when a single rain gauge is used in estimating areal mean rainfall. The
334 MAPE decreases by about 10% as the number of gauges increase until 5, then decrease by about 5% as the
335 number of gauges increase until 8. In addition, more than 8 rain gauges in Standard-basins make the effect of
336 the number of rain gauges small in estimating areal mean precipitation.

337 [Insert Figure 9]

338 The mean percentage error (MPE) is estimated as in Equation 5 and the results are presented in Figures 10 and
339 11:

$$340 \quad MPE_{ITP}^{RDR} = \frac{AMAR_{GRD}^{RDR} - AMAR_{ITP}^{RDR}}{AMAR_{GRD}^{RDR}} \times 100 \quad (5)$$

341 In common with MAPE results, as the number of rain gauges used in calculating areal mean annual rainfall
342 increases, the MPE between areal mean annual rainfall estimated from radar grid rainfall and four
343 interpolation methods decreases. However, unlike MAPE, MPE shows a clear trend according to the number
344 of rain gauges. IDW tends to underestimate (maximum mean 6.0%), while TSN tends to overestimate
345 (maximum mean 11.9%). KRG and MQI tend to overestimate a little when less than two rain gauges are used,
346 but when more than two rain gauges are used there is no clear bias trend overall. Figure 11 illustrates the mean
347 value of MPE extracted from Figure 10. Among 528 standard-basins, the proportion of the basins that have
348 rain gauges less than or equal to 4 per standard-basin are 70.5% and the rain gauges less than or equal to 6 per
349 standard basins are 94.9%. This indicates that, for example, when the TSN method is used, the error of the
350 estimated areal rainfall is about 5% in about 70% of standard-basins, and the error of the estimated areal
351 rainfall is about 3% in about 95% of standard-basins.

352 [Insert Figure 10]

353 [Insert Figure 11]

354

355 **4.2.3 Effects of rain gauge distribution**

356 It is evident from Figure 8 that MAPE decreases as the number of rain gauge used in calculating areal mean
357 rainfall increases. However, the mean value of MAPE (circle marks in Figure 8) appears irregularly at similar
358 numbers of rain gauges. From this, it can be assumed that there might be some other factors than the density
359 of rain gauges that affect areal mean rainfall estimation. Since the shape of catchments and locations of rain
360 gauges are fixed, it is reasonable to assume that this might be attributed to characteristics of rainfall that vary.
361 Although catchment shape and the number of rain gauges used are similar as illustrated in Figure 6, areal
362 mean rainfall could be substantially different due to the placement of rain gauges. The reason is that the

weight of each rain gauge differs according to the shape and movement of the areal distribution of rainfall. Moreover, as discussed in section 4.2.1, interpolation methods based on rain gauges such as TSN, areal mean rainfall could be overestimated due to a specific rain gauge rainfall if the density of rain gauge is low (i.e. rain gauges are far apart compared with cloud width) and the rainfall area is located over a particular rain gauge. On the other hand, in an area where there are no rain gauges, its area mean rainfall is likely to be poorly estimated. As a result, over- and underestimation of rainfall results, so that outliers occur repeatedly. To summarize, in this section, we examined the effects of rain gauge distribution patterns on estimated areal mean rainfall. In other words, the number of rainfall events that include outliers (i.e. extremely over- and under estimated values) are examined for different distributions of rain gauges. The linearity of a rain gauge distribution is measured by Spearman's correlation coefficient between the locations (i.e. latitude and longitude) of rain gauges. Figure 12 represents a schematic of the rain gauge distribution. When rain gauges are radially distributed as Figure 12(a), linear correlation coefficient among gauge locations is small, while in the case that rain gauges are linearly distributed as Figure 12(b), the linear correlation coefficient among gauge locations is large but, in the end, it is a function of interstation distance between them.

[Insert Figure 12]

To investigate whether or not outliers occur depending on the distribution of rain gauges, the relationship between frequency of outlier occurrence and rain gauge locations was estimated. An outlier is defined based on the so-called 'three sigma rule of thumb', i.e. estimated areal mean rainfall that lie within three standard deviations about the mean value are assumed as outliers. Sixty-one rainfall events at 664 Standard-basins, which are used in flood forecasting, were analysed.

In Figure 13, the green bar graph shows the number of rainfall events that include outliers (left y-axis) according to the correlation coefficients of the geometric distribution of gauges (x-axis) in the Standard-basin. The solid red lines represent the empirical cumulative distribution function (ECDF, right y-axis) of this bar graph series, and the pink dotted line represents 95% confidence interval of ECDF. The number of rainfall events with outliers increases as the correlation among rain gauge locations increases. This implies that outliers are more likely to happen when the gauges are located in a linear format. Especially, the slope of outlier occurrence changes from 0.83 to 1.44 before and after when the correlation coefficient is 0.7, which

means that the stronger the linearity of rain gauge distribution is, the bigger the tendency of the frequency of outliers' occurrence grows. Therefore, as expected, not only the rain gauge density but also the distribution of rain gauges influences the accuracy of areal mean rainfall estimation. In addition, the reason for the difference of MAPE between similar numbers of rain gauges in Figure 8 might be due to the problem of rain gauge distribution. This implies that the shape and distribution of rain gauges is important in order not to over- or underestimate areal mean rainfall at small catchments, as expected.

[Insert Figure 13]

4.2.4 Effects of rainfall direction

The distribution of rain gauges and movement of rainfall events not only affect the magnitude of areal mean rainfall but also the temporal distribution of areal mean rainfall. To investigate this, the occurrence time of peak rainfall was compared between time series of rain gauge based areal mean rainfall and radar based areal mean rainfall, at 10 minute intervals. Figure 14 shows an example of the time lag of peak rainfall occurrence depending on rain gauge placement and rainfall movement. The rain gauge is located outside the catchment on the bottom right of the 4 colored maps (black circle) in this Standard-basin (102307). The white arrows indicate the direction of rain storm. The storm happened between 00:00 (AM) to 12:00 (AM) on May 16, 2018. In the beginning of the rainfall event (time t and $t+1$), the storm is moving from right to left. Therefore, the peak areal mean rainfall from rain gauge (G^t, G^{t+1}) is estimated earlier than from radar data (R^t, R^{t+1}). However, at the end of the rainfall event (time t' and $t'+1$), storm is moving from left to right. Therefore, the peak areal mean rainfall from radar data ($R^{t'}, R^{t'+1}$) is estimated earlier than from rain gauge ($G^{t'}, G^{t'+1}$). In this case, the point rainfall is the same as the areal mean rainfall since only one rain gauge is located outside the catchment. Therefore, when the center of the storm passes the rain gauge, areal mean rainfall might be overestimated. This result could be another reason for irregular MAPE in Figure 8 among a similar number of rain gauges. It can be concluded from this result that in order to calculate accurate areal mean rainfall from gauges, not only the number of rain gauges but the isotropic and uniform placement of rain gauges is important.

[Insert Figure 14]

5. Conclusions

The main objective of this study was to assess the influence of catchment area, rain gauge density, rain gauge distribution and direction of rainfall movement on estimating areal mean rainfall, by comparing the result of four different spatial interpolation methods. The main results and conclusions can be summarized as follows:

- (1) MAPD (mean absolute percentage discrepancy) and catchment area are inversely proportional. In addition, MAPD between TSN (Thiessen polygons) and the other three interpolation schemes increase rapidly as catchment area becomes smaller when the catchment area is less than 500km^2 .
- (2) Regarding the influence of rain gauge density (i.e. the number of rain gauges in the catchment), the fewer the number of rain gauges used in calculating areal mean rainfall are, the larger the MAPD becomes. In our study, MAPD has a value of 20% when only one rain gauge is used in estimating areal mean rainfall. MAPD decreases to about 10% as the number of rain gauges increase to 5, then decreases to about 5% as the number of rain gauges increase to 8. In addition, more than 8 rain gauges per basin will only improve the estimation of mean annual precipitation discrepancy below 5%, which will be impractical.
- (3) The IDW method tends to underestimate areal mean rainfall while TSN tends to overestimate and is spatially biased in relatively sparse networks. Therefore, KRG and MQI are recommended in estimating areal mean rainfall on small catchments.
- (4) The number of rainfall events with outliers increases as the correlation among rain gauge locations (linearity of rain gauge distribution) increases. Especially, outliers increase steeply when correlation coefficients are over 0.7. This implies that outliers are more likely to happen when the gauges are located in a linear pattern. Therefore, considerations of spatial distribution of rain gauges is important in order not to over- or underestimate areal mean rainfall.
- (5) Depending on the direction of rainfall movement, temporal distributions of areal mean rainfall are different when comparing rain gauge and weather radar data, especially when catchments have sparse rain gauges if Thiessen polygons are used as interpolants.

In South Korea, the Thiessen polygon method, which is out-dated, is officially used for river flood forecasting. This study clearly demonstrates that there are practical limitations in estimating areal mean rainfall when rain

443 gauge rainfall data is obtained from small catchments. A possible solution of limitations in estimating areal
444 mean rainfall could be merging radar and gauge data. Neither of them is accurate, but the combination is
445 better than working with only the one or the other (Pegram, 2001; Sinclair and Pegram, 2005). In addition,
446 differences in areal mean rainfall have been presented when different interpolation methods are applied, which
447 can provide guidelines for which interpolation method should be selected for different conditions and how the
448 rain gauges should be distributed to improve the accuracy of areal mean rainfall estimates.

449 **Appendix I. List of Acronyms**

450 AWS Automatic weather stations

451 AMAR Areal mean annual rainfall

452 IDW Inverse distance weighting

453 IQR Interquartile range

454 KMA Korea Meteorological Administration

455 KRG Kriging

456 MAPD Mean absolute percentage discrepancy

457 MAPE Mean absolute percentage error

458 ME Ministry of Environment

459 MPE Mean percentage error

460 MQI Multiquadric interpolation

461 QPE Quantitative precipitation estimation

462 TSN Thiessen polygon

463

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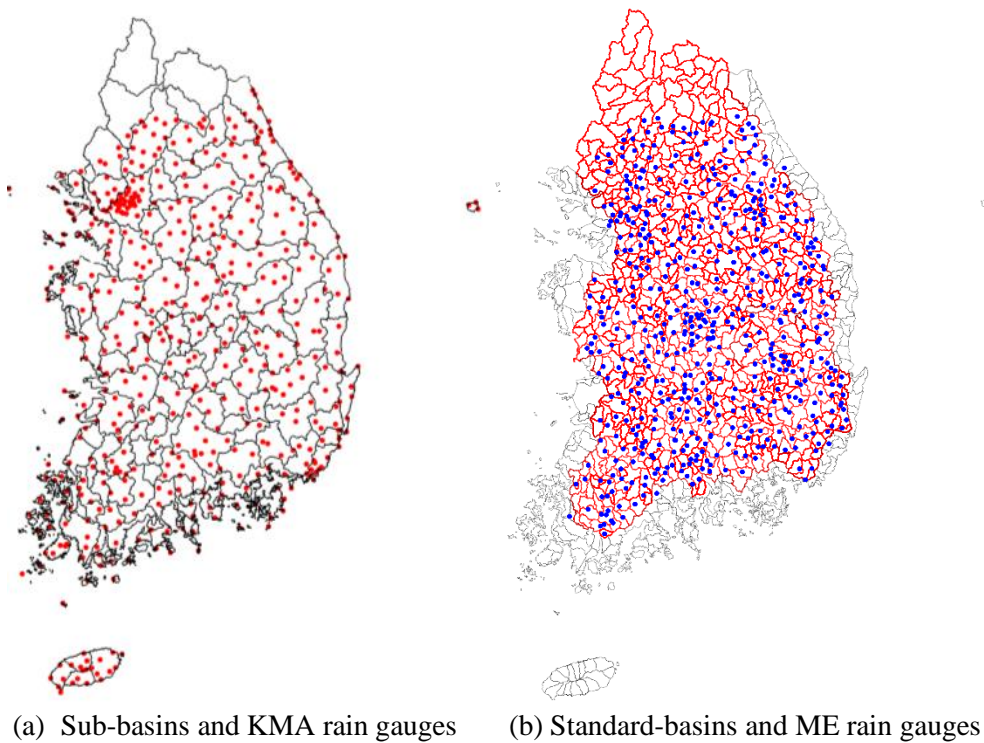
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573 universal kriging and inverse distance weighting. Mathematical Geology, 31(4): 375-390.

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582 Figure 1. (a) 117 Medium sized Sub-basins (black polygons) and Automatic Weather Stations (AWS) of the
583 Korea Meteorological Administration (KMA) (left red dots) for water management. (b) 850 Small sized
584 Standard-basins for flood forecasting. Red polygons (664 Standard-basins) represent the basins which are
585 used in river flood forecasting and blue dots are rain gauges installed by Ministry of Environment (ME).
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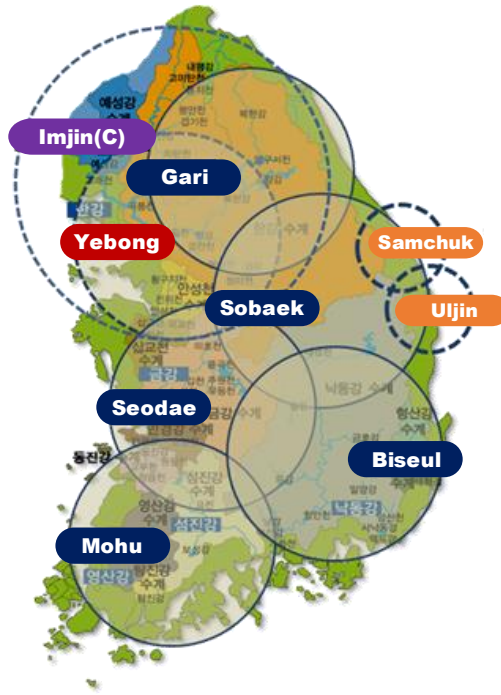


Figure 2. Locations and observation ranges of ME weather radars. Gari, Yebong, Sobaek, Seodae, Mohu, Biseul are S-band dual-polarization radars, Imjin(C) is a C-band single-polarization radar, and Samchuk, Uljin are small X-band radars for gap-filling large S-band radar networks.

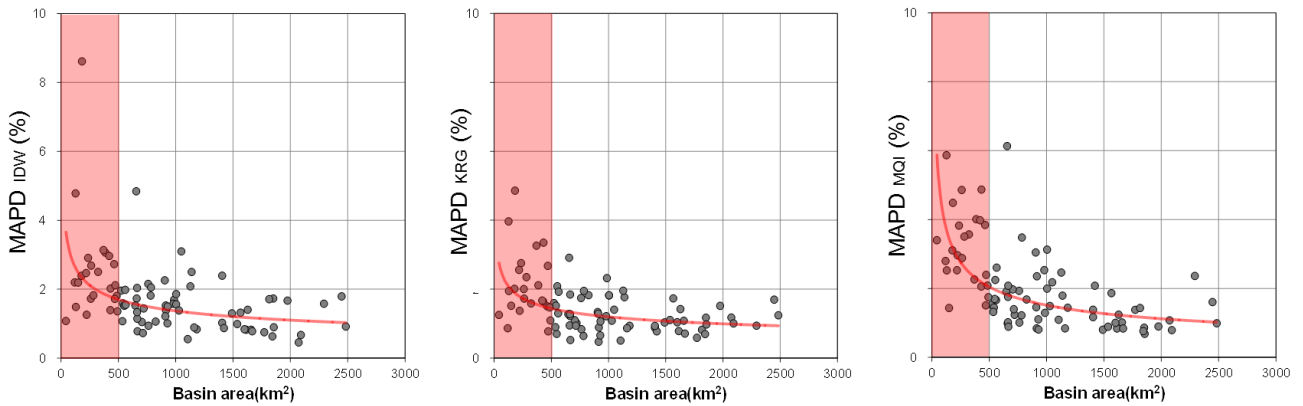


Figure 3. Mean absolute percentage discrepancy (MAPD) of areal mean annual rainfall for different spatial interpolation schemes and catchment areas. IDW, KRG and MQI represent Inverse Distance Weighting, Kriging and Multiquadric Interpolation respectively. The pink shading covers the smaller areas.

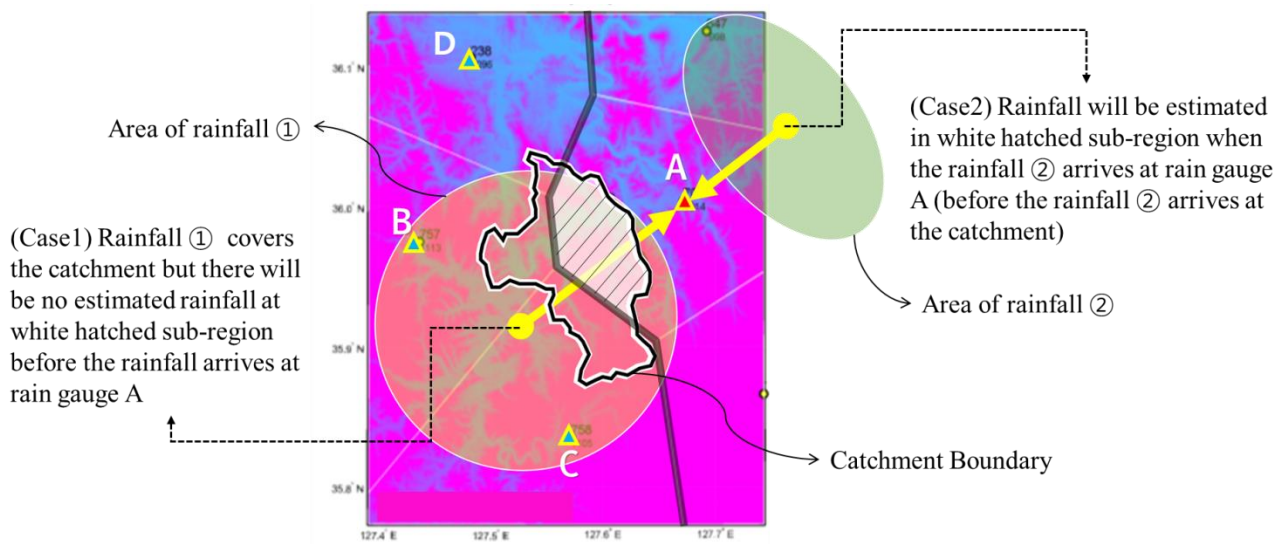
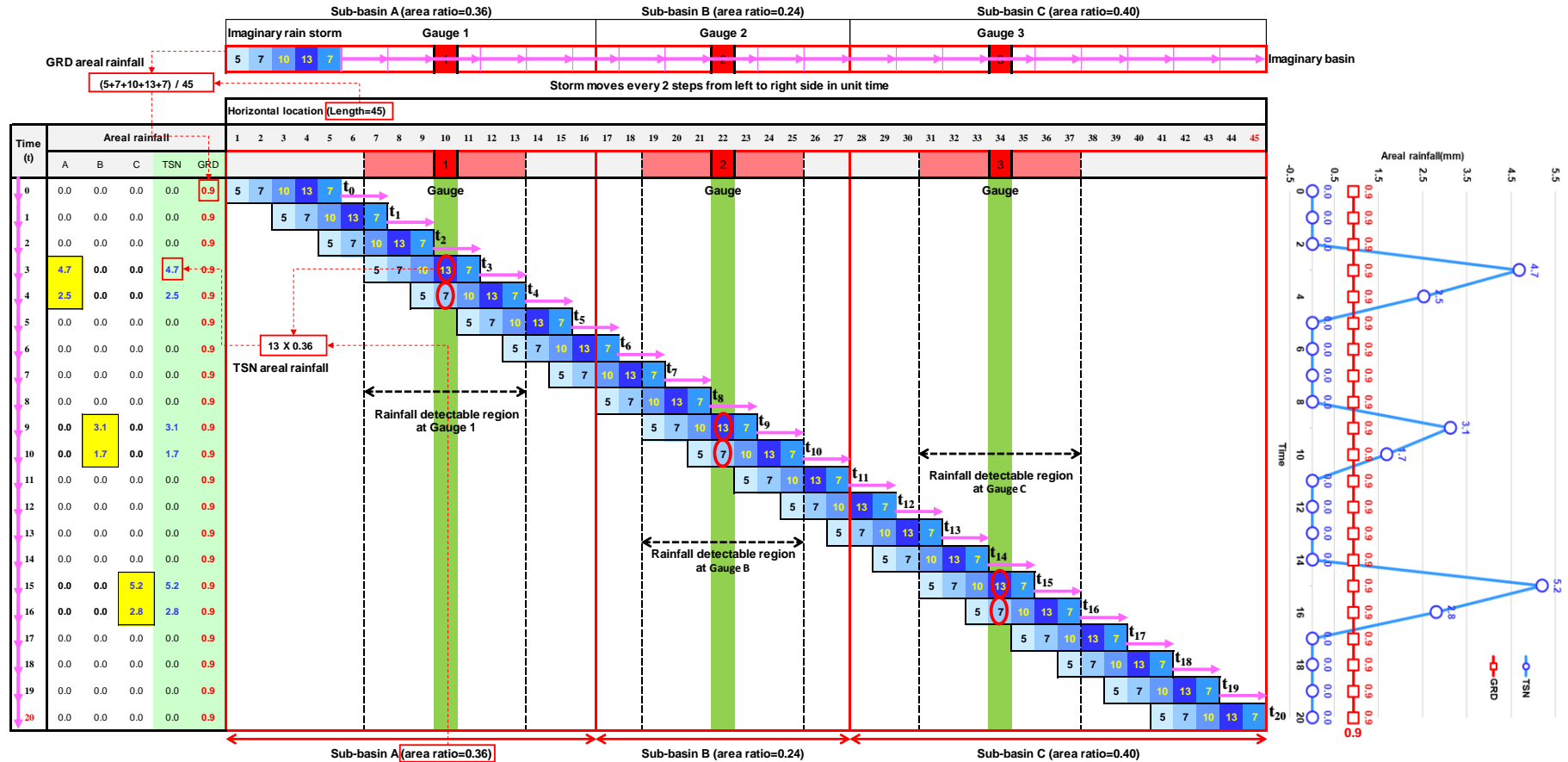


Figure 4. Illustration of the drawback of the Thiessen polygon method (TSN). An example of four rain gauges (A, B, C, D) located outside the catchment and the storm moving from South West to North East (Case 1) and vice versa (Case 2).



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609 Figure 5. Schematic example of rainfall movement and Thiessen polygon (TSN) method. This figure is an example showing the characteristics of
 610 precipitation calculated by the TSN when the distance between rain gauges are set further apart than the storm size. The example consists of hypothetical
 611 rainfall (rainfall distribution 5, 7, 10, 13, 7mm), three catchments (Sub-basin A, B, C) and three rain gauges (Gauge 1, 2, 3). The horizontal axis represents
 612 distance and the vertical axis represents time. Here, the units of time and distance are ignored because it is a hypothetical example. The figure represents that
 613 the imaginary rainfall at the top shifts by 2 steps in a unit time from 0 to 20 time steps. Red boxes 1, 2, and 3 indicate rainfall gauges, respectively. The line
 614 graph on the right panel shows areal mean rainfall over time calculated by the TSN method and the grid mean rainfall (GRD) method. The GRD is constant
 615 over time, while TSN is fluctuating sharply.

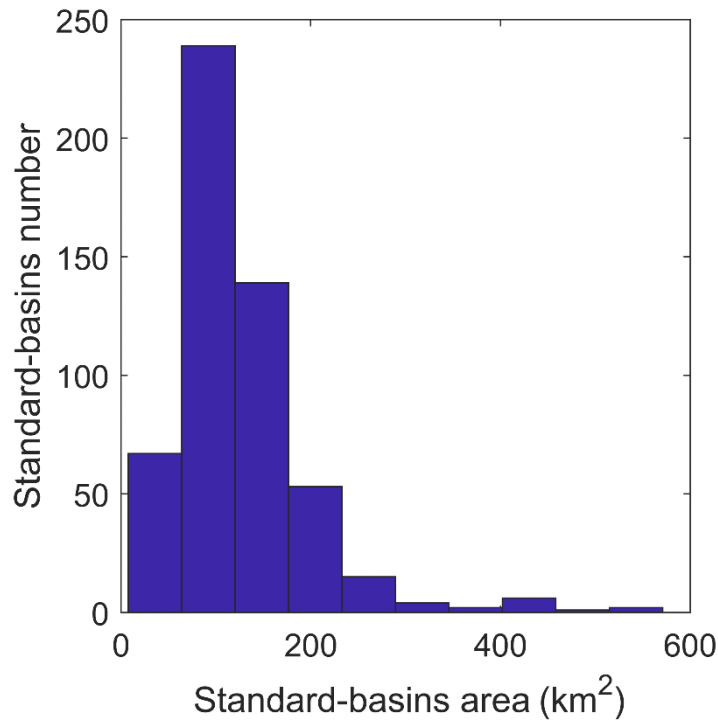


Figure 6. Areal distribution of 528 standard-basins. The mean value of 528 standard-basins area is 126 km².

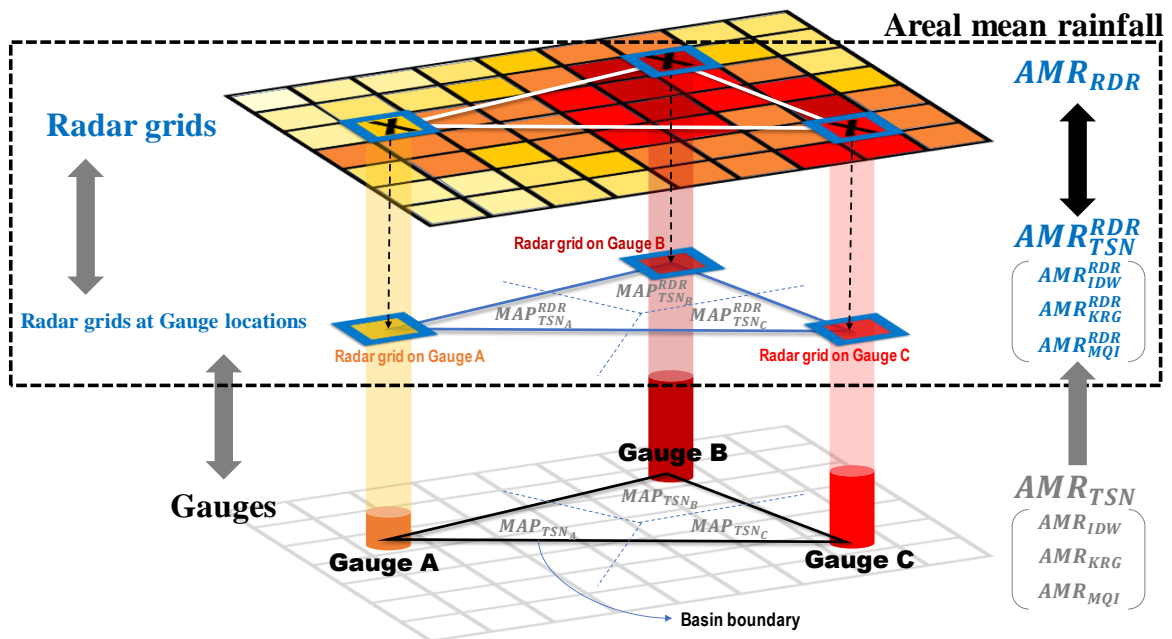
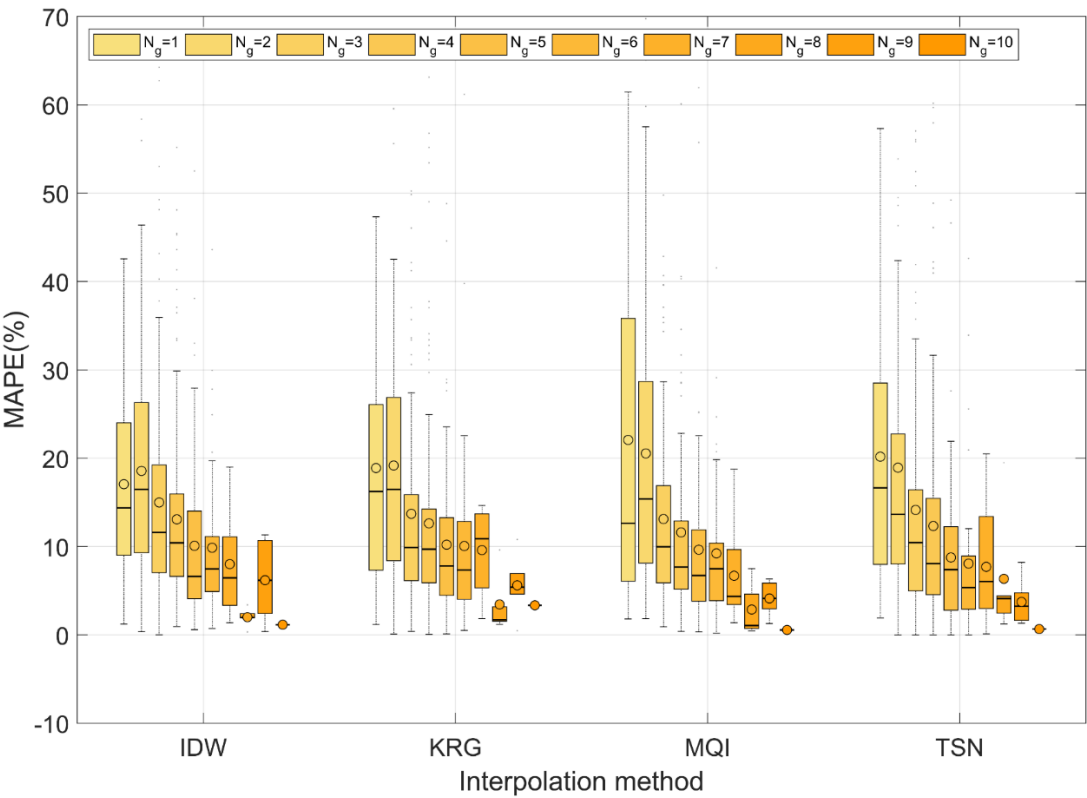


Figure 7. Schematic illustration of estimating areal mean rainfall with different interpolation methods using radar rainfall data. TSN, IDW, KRG and MQI are interpolation methods respectively. AMR_{GRD}^{RDR} is areal mean rainfall estimated from radar grid rainfall.



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626 Figure 8. Boxplots of mean absolute percentage error (MAPE, %) with respect to different number of rain
627 gauges (N_g) and different spatial interpolation methods. The horizontal line in the box represents the median
628 value and the black circle represents the mean value. The box height represents the 25th percentile (1st
629 quartile) to the 75th percentile (3rd quartile) of MAPE sets. The whiskers are the two lines outside the box that
630 extend to the highest and lowest values. IDW, KRG, MQI and TSN represent Inverse Distance Weighting,
631 Kriging, Multiquadric Interpolation and Thiessen polygon respectively.

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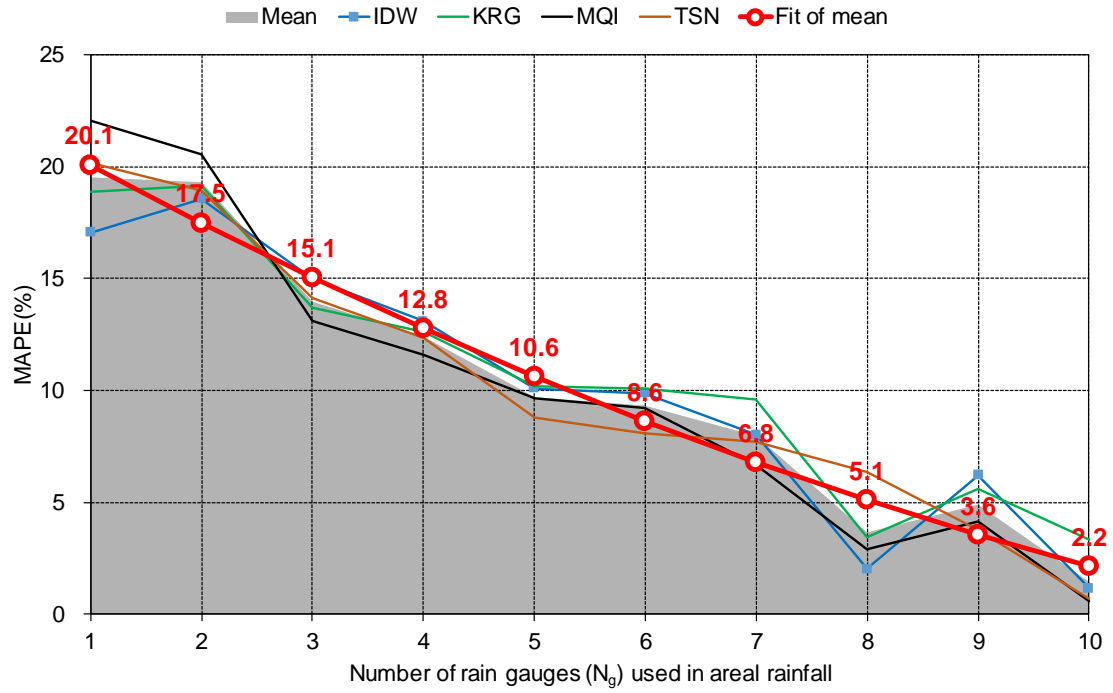


Figure 9. Mean value of MAPE (%) with respect to each number of rain gauges (N_g) in Figure 8. MAPE decreases for all interpolation methods as number of rain gauges increase.

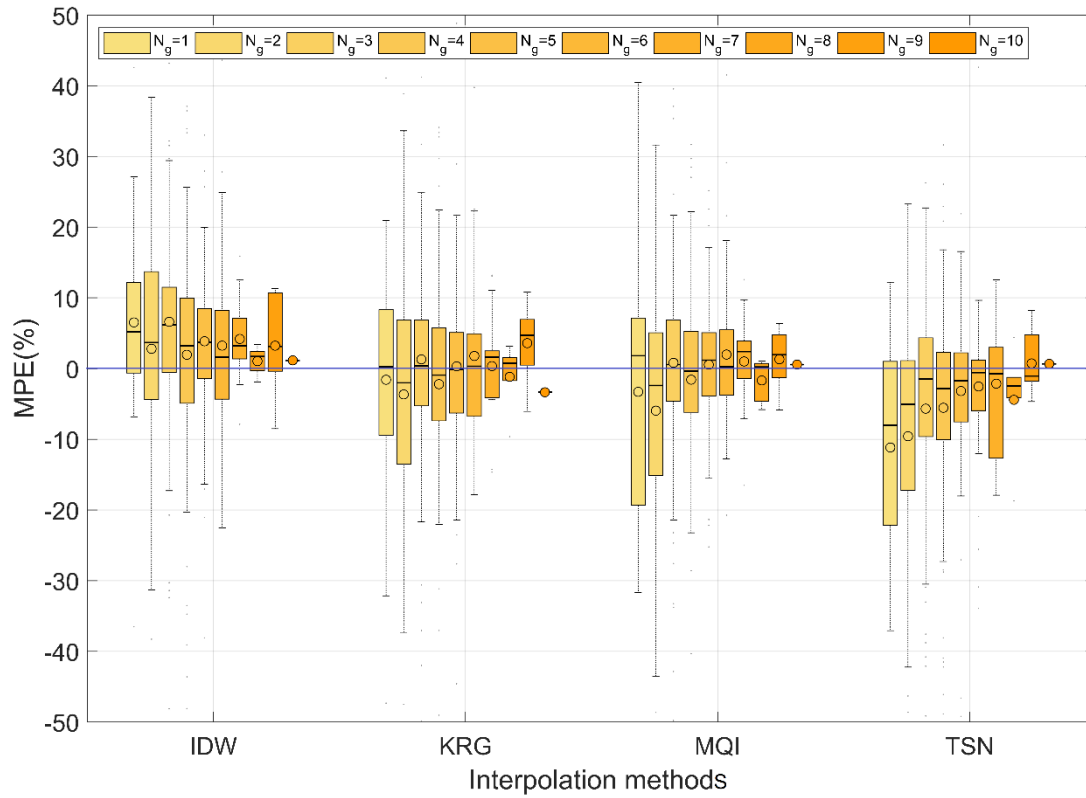


Figure 10. Boxplots of Mean percentage error (MPE, %) with respect to different number of rain gauges (N_g) and different spatial interpolation methods. The horizontal line in the box represents the median value and the black circle represents the mean value. The box height represents the 25th percentile (1st quartile) to the 75th percentile (3rd quartile) of MPE sets. The whiskers are the two lines outside the box that extend to the highest and lowest values. IDW, KRG, MQI and TSN represent Inverse Distance Weighting, Kriging, Multiquadric Interpolation and Thiessen polygon respectively.

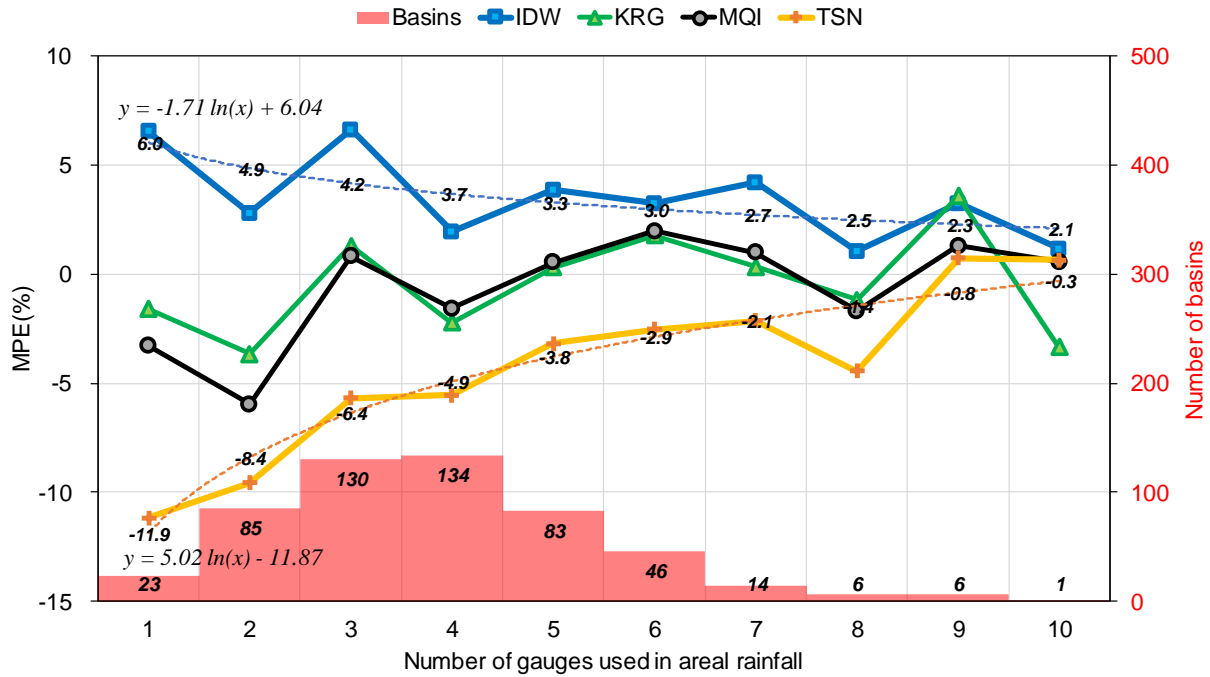


Figure 11. Mean value of MPE is extracted from Figure 10. Yellow line show MPE of TSN with respect to N_g , blue line show MPE of IDW, green line show MPE of KRG and black line show MPE of MQI. Red histogram shows the number of standard-basins. Blue dotted line is the fitted curve of MPE of IDW and yellow dotted line is the fitted curve of MPE of TSN.

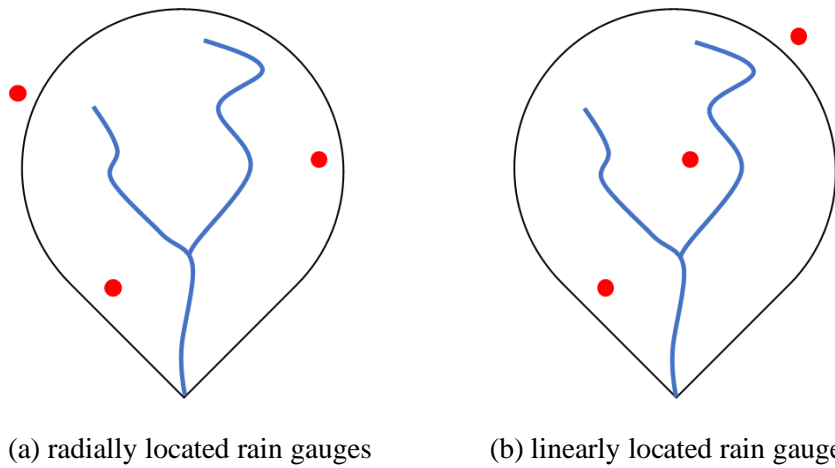
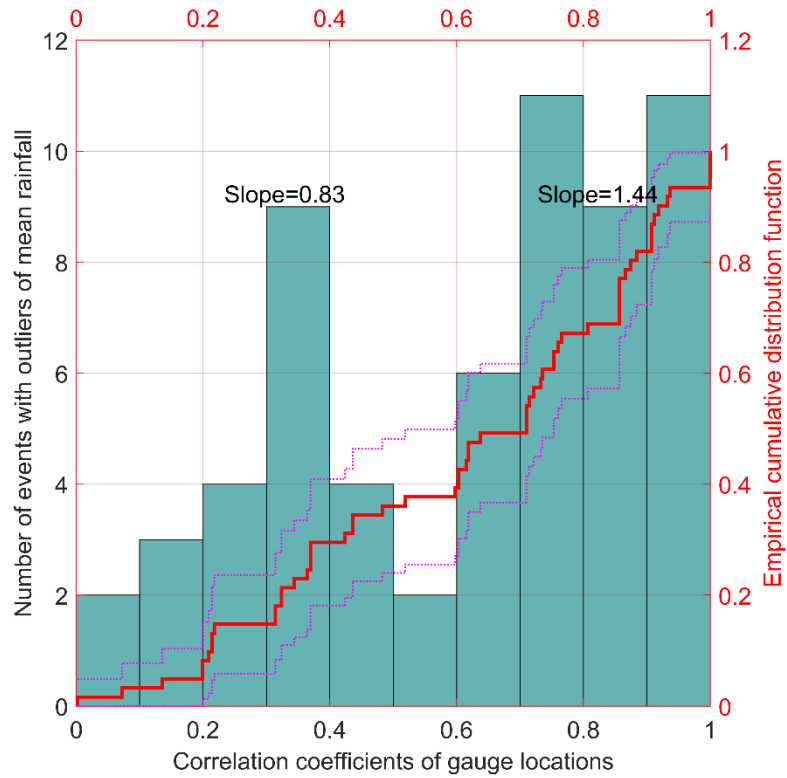


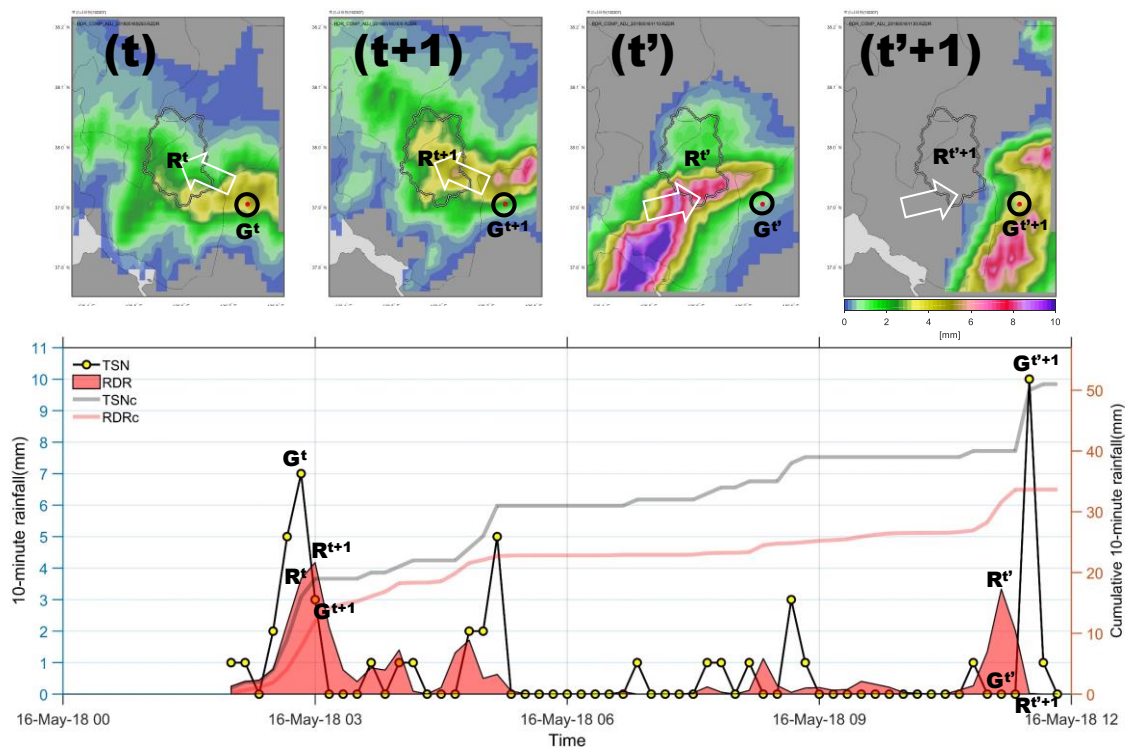
Figure 12. Schematic of rain gauge distribution. Black line is the boundary of hypothetical basin and red dots are rain gauges.



661

662 Figure 13. Relationship between number of areal mean rainfall outliers in 61 rainfall events and correlation
 663 coefficients of rain gauge geographic locations based on latitude and longitude in 664 Standard-basins. The
 664 solid red line represents the empirical cumulative distribution function (ECDF, right y-axis) of this bar graph
 665 series, and the pink dotted lines represent the 95% confidence interval of ECDF. The slope of outlier
 666 occurrence changes from 0.83 to 1.44 before and after when the correlation coefficient is 0.7.

667



670 Figure 14. An example showing the time lag of peak rainfall occurrence depending on the distribution of rain
671 gauges and rainfall movement on 15 May, 2018. The rain gauge is located outside the catchment on the
672 bottom right of the 4 colored maps (black circle in the upper panel). In the beginning of the rainfall event
673 (time t and $t + 1$, the sampling time interval is 10-minutes), the storm is moving from right to left , as shown
674 in the first two of the 4 panels above the time series, but changes direction about 9 hours later. The time-shift
675 in the two periods are lagged by distance as can be seen the lower panel.. The white arrows indicate the
676 direction of rainfall movement. TSN and RDR represent the areal rainfall using the Thiessen polygon method
677 and radar areal mean rainfall, respectively. TSNc and RDRc represent the cumulative areal rainfall using the
678 Thiessen polygon method and cumulative radar areal mean rainfall over the catchment, outlined in grey in the
679 upper 4 panels, respectively.
680